INVESTIGATING NONSTANDARD COSMOLOGICAL SCENARIOS: BIANCHI TYPE I MODELS WITH PERFECT FLUID WITHIN THE FRAMEWORK OF GENERAL RELATIVITY

Amit S. Patel and Priya R. Desai

School of Mathematics, Sprout Institute, New Delhi University, India Abstract: The exploration of spatially homogeneous and anisotropic universes, particularly those exhibiting tilt, has garnered significant interest in recent years. Tilted universes, where matter does not move orthogonally to the hypersurface of homogeneity, offer a nuanced understanding of cosmic dynamics. Early seminal works by King and Ellis (1973), Ellis and King (1974), and Collins and Ellis (1979) extensively examined the general dynamics of tilted universes. Dunn and Tupper (1978) and Lorenz (1981) specifically delved into Tilted Bianchi Type I models, while Mukherjee (1983) investigated these universes with heat flux, revealing intriguing pancake-shaped configurations. Bradley (1988) contributed by deriving tilted spherically symmetric self-similar dust models, adding to the complexity of equations governing tilted cosmological scenarios.

The mathematical formalism governing tilted cosmological models is notably intricate compared to non-tilted ones, as highlighted by Ellis and Baldwin (1984), who proposed the potential presence of tilt in our universe and suggested detection methods. Further advancements include the exploration of tilted cold dark matter cosmological scenarios by Cen et al. (1992), shedding light on the implications of tilt in cosmological dynamics. Additionally, Bali and Sharma (2002) delved into the characteristics of tilted Bianchi Type I dust fluid, revealing peculiar cigar-type singularities under certain conditions.

This abstract encapsulates the evolving landscape of tilted universes, emphasizing the significance of tilt in shaping cosmic evolution and structure. Through a historical overview and examination of key findings, it underscores the importance of understanding tilted cosmological models in elucidating fundamental aspects of the universe's evolution and structure.

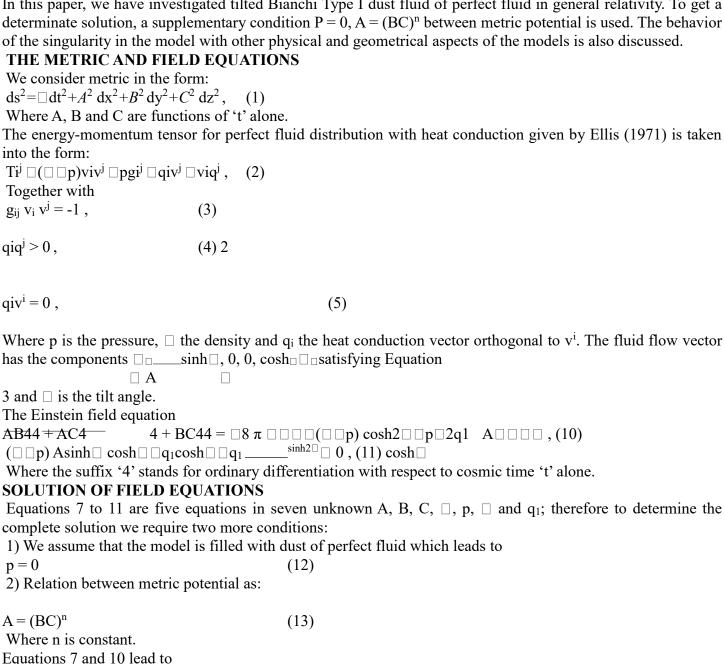
Keywords: Tilted universes, cosmological dynamics, Bianchi Type I models, cosmic evolution, cosmic structure

INTRODUCTION

In recent years, there has been a considerable interest in investigating spatially homogeneous and anisotropic universe in which the matter does not move orthogonally to the hypersurface of homogeneity. These are called tilted universe. The general dynamics of tilted universe have been studied in detail by King and Ellis (1973), Ellis and King (1974), and Collins and Ellis (1979). Tilted Bianchi Type I models have been obtained by Dunn and Tupper (1978) and Lorenz (1981). Mukherjee (1983) has investigated tilted Bianchi Type I universe with heat

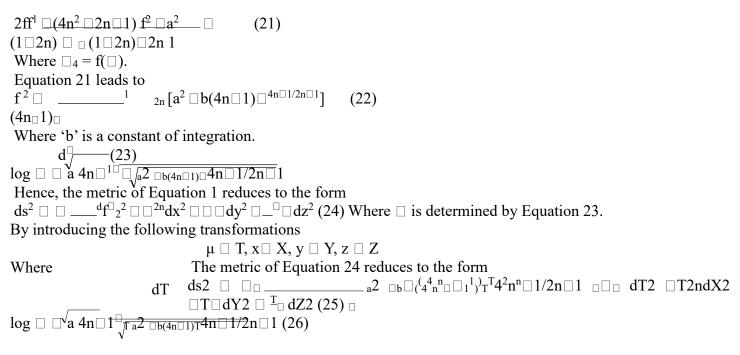
flux in general relativity. He has shown that the universe assumes a pancake shape. Bradley (1988) obtained all tilted spherically symmetric self-similar dust models. The equations for tilted cosmological models are more complicated than those of non-tilted ones. Ellis and Baldwin (1984) have shown that we are likely to be living in a tilted universe and they have indicated how we may detect it. A tilted cold dark matter cosmological scenario has been discussed by Cen et al. (1992). Bali and Sharma (2002) investigated tilted Bianchi Type I dust fluid and shown that model has cigar type singularity when T = 0.

In this paper, we have investigated tilted Bianchi Type I dust fluid of perfect fluid in general relativity. To get a determinate solution, a supplementary condition P = 0, $A = (BC)^n$ between metric potential is used. The behavior of the singularity in the model with other physical and geometrical aspects of the models is also discussed.



B44 C44 2B4C4 □ A4C4 □ A4B4 □ 8 □ (□□p) □ □	(14)	
Rij $\Box 1$ Rgij $\Box \Box 8 \Box T$ ij, (units such that $c = G$	= 1) (6)	
For the line, element of Equation 1 are		
B44 + C44 + B4C4 = $\square 8 \pi \square \square (\square \square p) \sinh 2$ B C BC \square $\sinh \square$, (7)	.□ □p□2q1	
$A \square \square$		
$A44 + C44 + A4C4 = \square 8\pi p$,		
A C AC		
(8)		
$A44 + B44 + A4B4 = \Box 8\pi p$,		
A B AB		
(9)		
AB AC BC sinh		
B C BC AC AB		
From Equations 12 and 14, we have $^{\text{B}}_{44} \ ^{\text{C}}_{4} \ ^{\text{B}}_{4} \ ^{\text{C}}_{4} \ ^{\text{A}}_{4} \ ^{\text{C}}_{4} \ ^{\text{A}}_{4} \ ^{\text{C}}_{4} \ ^{\text{A}}_{4} \ ^{\text{C}}_{4} \ ^{\text{B}}_{4} \ ^{\text{C}}_{4} \ ^{\text{C}}$	5)	
B C BC AC AB	,	
Equations 8 and 9 lead to		
$\overset{B}{_{44}} \ \overset{C}{_{44}} \ \overset{A}{_{4}} \ \overset{A}{_{4}} \ \overset{B}{_{4}} \ \overset{C}{_{4}} \ \overset{C}{\overset{C}} \ \overset{C}} \ \overset{C}} \ \overset{C}{\overset{C}} \ \overset{C}{\overset{C}} \ \overset{C}{\overset{C}} \ $	(16)	
$\mathbf{B} \mathbf{C} \mathbf{A} \square \mathbf{B} \mathbf{C} \square$		
This leads to		
$\frac{\Box 4}{\Box} \Box \frac{a}{n} \Box 1$	(17)	
Where BC = \square , $\underline{B}_{\square\square}$ and 'a' is constant of in	itegration.	
C		
Again from Equations 8 and 9, we have		
$2A44 \square B44 \square C44 \square A4C4 \square A4B4 \square \square$	16□p (18)	
A B C AC AB		
From Equations 12 and 18, we have		
2A44 \square B44 \square C44 \square A4C4 \square A4B4 \square 0	(19)	
A B C AC AB		
Equation 19 gives		
2 2	_	
2(1 ₀ 2n)044 ₀ (4n2 ₀ 2n ₀ 1) ⁰ _04 ₀ 000	$\Box 4 \Box \Box \Box 0$ (2	0)
Where $A = \Box^n$.		
From Equations 17 and 20, we have		

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SOME PHYSICAL AND GEOMETRICAL FEATURES

The density for the model of Equation 25 is given by:

(ii)
$$\Box + 3p > 0$$
, lead to $b(4n \Box 1) T^{\frac{-(4d)^2(2n+1)}{(2n+1)}} \Box 0$ (30)

 $2(2n\square 1)$

Where

 $b(4n \square 1)$

____⊓ 0

 $2(2n\square 1)$

The scalar of expansion \square calculated for the flow vector \square^i is given by:

The components of fluid flow vector vi and heat Bagora and Bagora 3 conduction vector qi for the model of Equation 25 are given by:

$$\Box^{1} \Box \frac{1}{2T^{n}} \sqrt{\frac{1 \Box 2n}{n}}$$
 (32)

$$\Box^{4} \Box \frac{1}{2} \sqrt{\frac{2n \Box 1}{n}} \tag{33}$$

 $64\square(2n\square1)T$

The non-vanishing components of shear tensor (\Box_{ij}) and rotation tensor (\Box_{ij}) are given by $(4n^2 \square 1) (2n \square 1) \square a^2 \square b (4n \square 1) T^{4n \square 1/2n \square 1} \square (36)$

 $\Box 14 \Box \Box$

$$\begin{array}{ccc} 24nT & n \\ (40) & \\ \omega_{14} = (6n \square 1) \ (1 \square 2n) \square a^2 \ \square b (4n \square 1) T^{4n \square 1/2n \square 1} \square \ (41) \\ 16T & n(4n \square 1) \end{array}$$

The rates of expansion
$$H_i$$
 in the direction of x , y and z axes are given by
$$H_1 \underset{\square}{\square} \frac{n}{T^{8n^2} \square^{4n} \square^{1/2(2n} \square^{1)}} \sqrt{\frac{a^2 T^{4n^2} \square^{2n} \square^{1/(4n} \square^{1)}}{4n} \underset{\square}{\square} \frac{b(4n}{\square} 1) T^{2n}} \qquad \text{(42)}$$

$$H_{2} \prod_{2T^{8n^{2}}\square^{4n}\square^{1/2(2n}\square^{1)}} \sqrt{\frac{a^{2}T^{4n^{2}}\square^{2n}\square^{1/(4n}\square^{1)}}{4n} \prod_{1} b(4n} \square^{1)} \frac{a}{2T^{n}\square^{1}}} \prod_{2T^{n}\square^{1}} (43)$$

$$H_{3} \underset{\square}{\Pi} \frac{1}{2T^{8n^{2}} \square^{4n} \square^{1/2(2n} \square^{l)}} \sqrt{\frac{a^{2}T^{4n^{2}} \square^{2n} \square^{1/(4n} \square^{l)}}{4n} \underset{\square}{\Pi} b (4n \underset{\square}{\Pi} l) T^{2n}}{1}} \underset{\square}{\Pi} \frac{a}{2T^{n} \square^{l}} \tag{44}$$

DISCUSSION

The model started with a big-bang at T = 0 and the expansion in the model decrease as time T increases and it stopped at $T = \square$. The model has point type singularity at T = 0 (MacCallum, 1971). The model represents shearing and rotating universe in general and rotation goes on decrease as time increases. Since $\lim_{\infty} 0$, then the model does not approach isotropy

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$T \; \square \; \square$
for large value of T.
Density \square \square 0 as T \square \square and \square \square as T \square 0. When T \square 0. q^1 \square and q^4 \square . Also, q^1 and q^4 tend to zero as T
\square 0. At T = 0, the Hubble parameters tend to infinite at the time of initial singularity of vanish as T \square \square .
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